Mass spectrometry analysis gives a series of peak height readings for various ion masses. For each peak the height $h_{j}$ is contributed to by the various constituents. These make different contributions $c_{i j}$ per unit concentration $p_{i}$ with the relation:

$$
h_{j}=\sum_{i=1}^{n} c_{i j} p_{i}
$$

* taken, but somewhat modified, from Curtis F. Gerald, Patrick O. Wheatley Applied Numerical Analysis

A sample returns peak heights: $h=(5.2,61.7,149.2,79.4,89.3)$.
What is concentration $p_{i}$ for each component, where the contributions $c_{i j}$ are given in the following table.

Component

| Peak <br> number | $\mathbf{C H}_{4}$ | $\mathbf{C}_{\mathbf{2}} \mathbf{H}_{\mathbf{4}}$ | $\mathbf{C}_{\mathbf{2}} \mathbf{H}_{\mathbf{6}}$ | $\mathbf{C}_{\mathbf{3}} \mathbf{H}_{\mathbf{6}}$ | $\mathbf{C}_{\mathbf{3}} \mathbf{H}_{\mathbf{8}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| 1 | 0.165 | 0.202 | 0.317 | 0.234 | 0.182 |
| 2 | 27.7 | 0.862 | 0.062 | 0.073 | 0.131 |
| 3 |  | 22.35 | 13.05 | 4.420 | 6.001 |
| 4 |  |  | 11.28 | 0 | 1.110 |
| 5 |  |  |  | 9.850 | 1.684 |

Mas


Mass spectrometry facilities and proteomics lab


Protein Function Discovery Facility $6^{\text {th }}$ Floor Botterell Hall


## BCHM 410/810 Lecture 3



A sample returns peak heights:
$h=(5.2,61.7,149.2,79.4,89.3)$
What is concentration $p_{i}$ for each component, where the contributions $c_{i j}$ are given in the following table.

|  | Component |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Peak <br> number | $\mathrm{CH}_{4}$ | $\mathrm{C}_{\mathbf{2}} \mathbf{H}_{\mathbf{4}}$ | $\mathrm{C}_{\mathbf{2}} \mathbf{H}_{\mathbf{6}}$ | $\mathbf{C}_{\mathbf{3}} \mathbf{H}_{\mathbf{6}}$ | $\mathbf{C}_{\mathbf{3}} \mathbf{H}_{\mathbf{8}}$ |
|  |  | 0.202 | 0.317 | 0.234 |  |
| 1 | 0.165 | 0.862 | 0.062 | 0.073 | 0.182 |
| 2 | 27.7 | 22.35 | 13.05 | 4.420 | 6.001 |
| 3 |  |  | 11.28 | 0 | 1.110 |
| 4 |  |  | 9.850 | 1.684 |  |

We can formulate this problem as a system of linear equations.
$A=0.1650$
27.7000
0.2020
0.8620
22.3500
0
0
0.3170
0.0620
0.2340
0.1820
13.0500
11.2800
0.0730
0.1310
$\begin{array}{lr}0 & 22.3500 \\ 0 & 0 \\ 0 & 0\end{array}$
11.2800
4.4200
0
6.0010
1.1100
$h=(5.2,61.7,149.2,79.4,89.3)^{T}$

Given the linear system $A p=h$, we need to solve for $p$. We could use Gaussian elimination.

In Matlab this is very easy to do, using the "magic" $\backslash$ (forward slash also know as left division) operator .
$A=\left[\begin{array}{llllll}0.165 & 0.202 & 0.317 & 0.234 & 0.182 ;\end{array}\right.$
27.70 .8620 .0620 .0730 .131 ;
022.3513 .054 .4206 .001 ;
$0011.2801 .110 ; 0009.851 .684]$
$h=\left[\begin{array}{lllll}5.2 & 71.9 & 149.2 & 79.4 & 89.3\end{array}\right]^{\prime}$
$\mathrm{p}=\mathrm{A} \backslash \mathrm{h}$

For the next week or so we will look at various means of solving systems of linear equations.

By the way the concentrations of the components turn out to be:

$$
\mathrm{p}=\begin{array}{ccccc}
\mathrm{CH}_{4} & \mathrm{C}_{2} \mathrm{H}_{4} & \mathrm{C}_{2} \mathrm{H}_{6} & \mathrm{C}_{3} \mathrm{H}_{6} & \mathrm{C}_{3} \mathrm{H}_{8} \\
\hline 2.5373 & 0.1288 & 6.6815 & 8.4449 & 3.6329
\end{array}
$$

